

# Indian Institute of Technology, Kharagpur

Time: 3 Hours  
End Semester Examination

Full Marks: 50  
Autumn, 2012-2013

No. of students: 56  
Department: Chemistry

Subject: **CY41007 GROUP THEORY FOR CHEMISTS**

1. Answer all questions.
2. If specified, answers **MUST** be tabulated in the format shown followed by the details of calculations, if any.

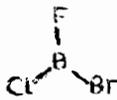
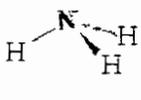
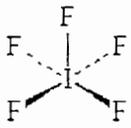
Q.1. Complete the following tables in your answer script.

5+5=10

a.

Symmetry point group	Schönflies notation
(i) Non-rotational group with a center of inversion	
(ii) Cubic group without a center of inversion	
(iii) Single axis rotational group of order $n$ with $\sigma_h$	
(iv) Group obtained by adding inversion $i$ to $C_3$	
(v) Group generated by $S_n$ axis ( $n$ odd)	

b.

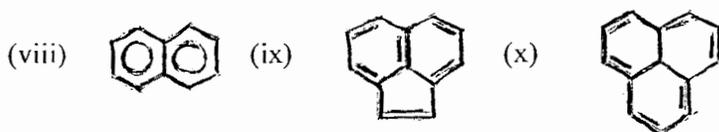
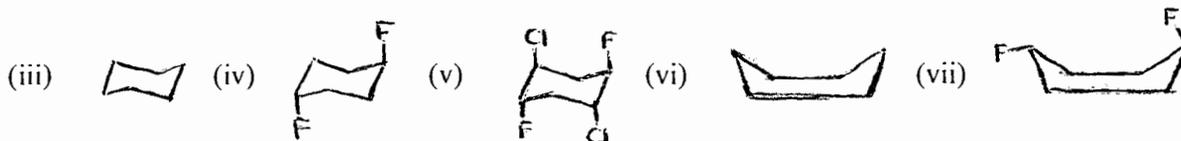
Molecule					
Number of $\sigma_v$ planes in the molecule					

Q.2. Write down the symmetry point groups of the following molecules in the tabular format shown.

Molecule	Symmetry point group
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1X10=10

- (i)  $MX_3$  trigonal planar (undistorted);    (ii)  $MX_3$  trigonal planar (distorted by lifting M out of plane)



Q.3. Describe in brief the implied symmetry properties of the irreducible representations on the basis of their Mulliken symbols. 1X5=5

- (i)  $A_g$  in  $C_{2h}$
- (ii)  $E_u$  in  $D_{3d}$
- (iii)  $A_2$  in  $D_{3h}$
- (iv)  $B_{1g}$  in  $D_{4h}$
- (v)  $E$  in  $D_{3h}$

Q.4. For the point group  $C_{2h}$ , answer the following questions. In each case, **briefly** state any rule/theorem that you may be using to obtain the answer, 25

- (i) Write down the complete list of symmetry operations in this point group. 2
- (ii) Obtain the group multiplication table. 2
- (iii) Show that there are four classes in this group. List the members of each class. 2
- (iv) Fill in the empty boxes in the character table given below. 2

$C_{2h}$				
$A_g$	1	1	1	1
$B_u$	1			
$A_u$	1			
$B_g$	1			

- (v) Consider a general vector,  $\vec{v}$  whose base is at (0,0,0) and whose tip is at (x,y,z) in the point group  $C_{2h}$ . Derive the set of four 3X3 transformation matrices that constitute the reducible representation,  $\Gamma_m$  by which  $\vec{v}$  transforms. 4
  - (vi) Show that the group of matrices comprising  $\Gamma_m$  is homomorphic with the group  $C_{2h}$ . 2
  - (vii) Reduce  $\Gamma_m$  into its irreducible representations by block diagonalization. 2
  - (viii) Write the reducible representation of characters,  $\Gamma_v$  that corresponds to the matrix representation  $\Gamma_m$ . 2
  - (ix) Show that  $\Gamma_v$  reduces to the same irreducible representations as  $\Gamma_m$ . 4
  - (x) Using the results from above, obtain the symmetry adapted basis function for the irreducible representation  $A_u$ . 3
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