

RA INDIAN INSTITUTE OF TECHNOLOGY, KHARAGPUR

Date: .11.2011 () Time: 3 Hrs. Full Marks: 80 Deptt: Physics & Meteo.

No. of Students 630, End Autumn Semester Examination

Sub. No. PH_11001 Sub. Name Physics-I

The paper contains 11 questions in one page. Each question carries 10 marks. Answer ANY EIGHT (8).

1. A grating has 800 lines/cm. Calculate the minimum width of the grating required to resolve the components of Sodium D-lines of wavelengths 5890 Å and 5896 Å respectively in the 2nd order.
2. For oblique incidence, the grating equation is $d(\sin\theta_i + \sin\theta_m) = m\lambda$, where θ_i and θ_m are respectively the angles of incidence and m^{th} order diffraction. What is the angle of minimum deviation for m^{th} order diffraction? If the angle of minimum deviation in the 1st order spectrum is 20° for mercury blue line of $\lambda = 4358$ Å, determine the number of lines per cm of the grating.
3. Write down the Schrodinger's equation for a free electron. Obtain the solution that describes the wavefunction for the free electron. Determine the electron's de Broglie wavelength and momentum (in terms of c) when $k = 50 \text{ nm}^{-1}$.
4. Explain how a Michelson interferometer is used to find the difference in wavelengths of D₁ and D₂ lines in Na-spectrum. The displacement of the movable mirror between two consecutive positions of maximum distinctness for D₁ and D₂ lines is found as 2.89×10^{-5} cm. Calculate $\Delta\lambda$.
5. Consider a plane wave of $\lambda = 0.60 \mu\text{m}$ incident normally on a long narrow slit of width 0.02 cm. The Fraunhofer diffraction pattern is observed on the focal plane of a lens of focal length 20 cm. Determine the positions and relative (as compared with the central maxima) intensities of the 1st and 2nd maxima.
6. A Compton collision occurs in which the photon is back-scattered *i.e.*, making an angle of 180° with the direction of incident photon. The scattered photon has **half** the energy of the incident photon. Find the wavelength of scattered photon in terms of Compton wavelength $\lambda_c = h/m_0c$. Calculate the de Broglie wavelength of the scattered electron.
7. Consider a double-slit diffraction pattern with $a = 0.008$ cm and $b = 0.07$ cm and $\lambda = 0.6328 \mu\text{m}$. Determine the number of minima between the two 1st order diffraction minima on either side of the principal maxima.
8. A thermal neutron has a speed v at temperature $T = 300\text{K}$ and kinetic energy given by $\frac{1}{2}mv^2 = 3kT/2$. Calculate its de-Broglie wavelength. What should be the inter-planar separation of a crystal for this beam of neutrons to be used for carrying out diffraction experiment? Assume $m = 1.67 \times 10^{-27}$ kg and $k = 1.38 \times 10^{-23} \text{ m}^2\text{kgs}^{-2}\text{K}^{-1}$.
9. A particle is in the ground state of an infinite potential well with length L . Calculate the probability that this particle will be found in the middle-half of the well, that is between $x = L/4$ to $x = 3L/4$.
10. Using Heisenberg's uncertainty principle estimate the minimum energy of a particle in one-dimensional simple harmonic potential, $V(x) = \frac{1}{2}kx^2$ such that total energy is $E = \text{K.E.} + \text{P.E.} = \frac{1}{2}p_x^2/m + \frac{1}{2}kx^2$.
11. The reflection coefficient of the two mirrors of a Fabry-Perot interferometer is $r = 0.8$ and the mirror separation is $d = 2.5$ cm. What are the nearest wavelengths on either side of $\lambda = 5000$ Å that can be resolved by this etalon?